

Rubin Observatory

PSF modeling plans Josh Meyers (LLNL)

Rubin Observatory Algorithms Workshop | Earth | March 17-19,
2020



Existing DM PSF framework

- Most widely used algorithm is PSFex
- Limited to running 1 sensor at a time
- We know we'll need to iterate for chromatic effects:
 - Initial PSF -> photometry -> better chromatic PSF
- Intend to include differential chromatic refraction as part of PSF (as opposed to WCS, where only DCR 1st moment could ever be included).



The goal for the future: a modular PSF

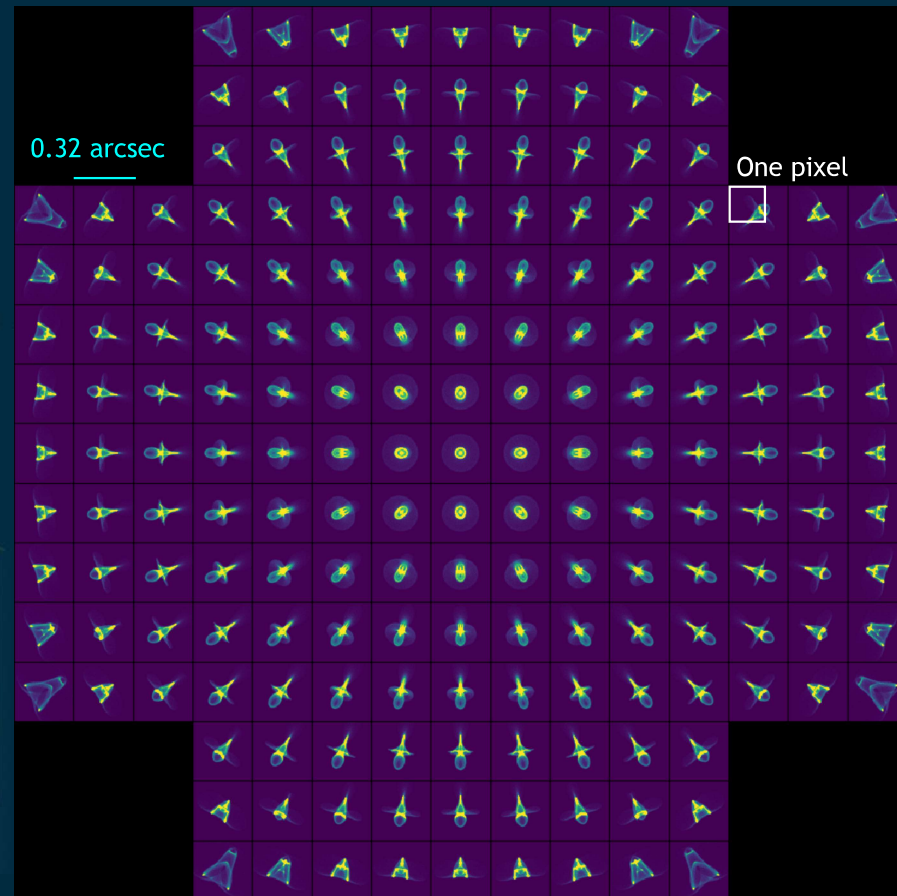
- PSF = Convolve(atmosphere, optics, CCD)
- Advantages:
 - **Robust**: small number of variables to describe full-field optics variations
 - Capture **chip discontinuities** in static optics PSF, allowing atmospheric PSF to be interpolated across entire focal plane
 - Easier modeling of PSF **chromaticity**, we have good models for how individual components behave chromatically.



A challenge: discontinuities

- Current PSF packages: fit individual stars using parametric model, interpolate coefficients
- CCD gaps => discontinuities
 - Limits packages to working one CCD at a time.
- Uniform distribution of heights between +/- 5 microns leads to size discontinuities of ~1% after convolution with atmosphere, sensor PSF contributions.

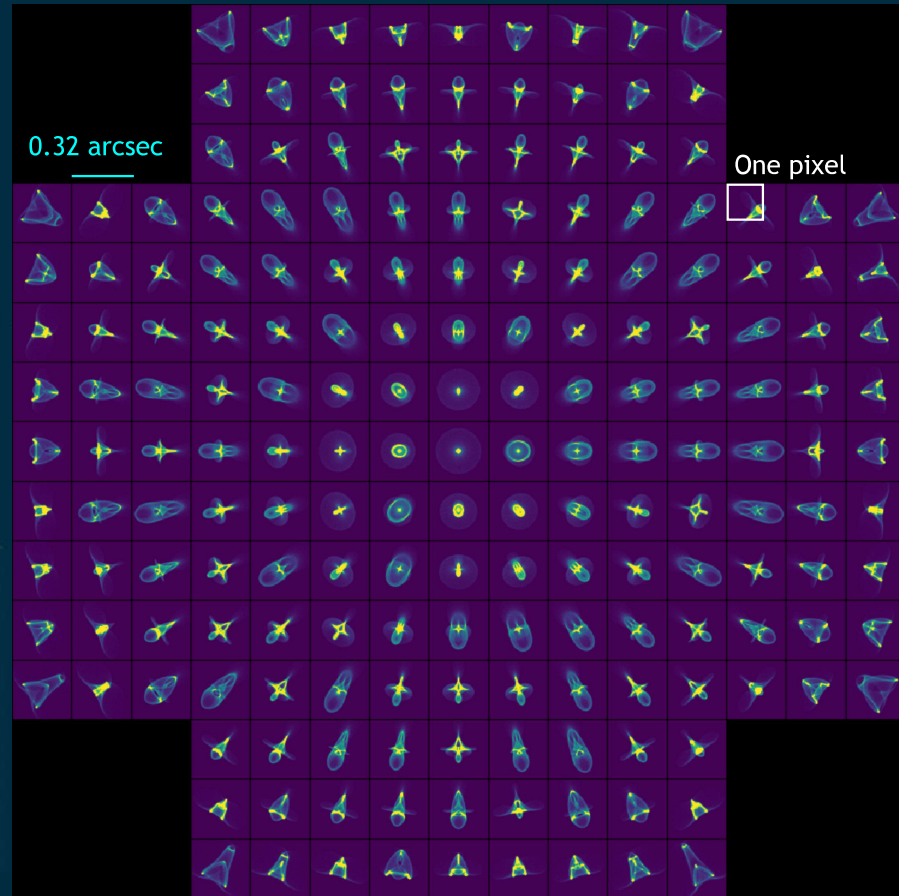
Fiducial Rubin Obs optical PSF



A challenge: discontinuities

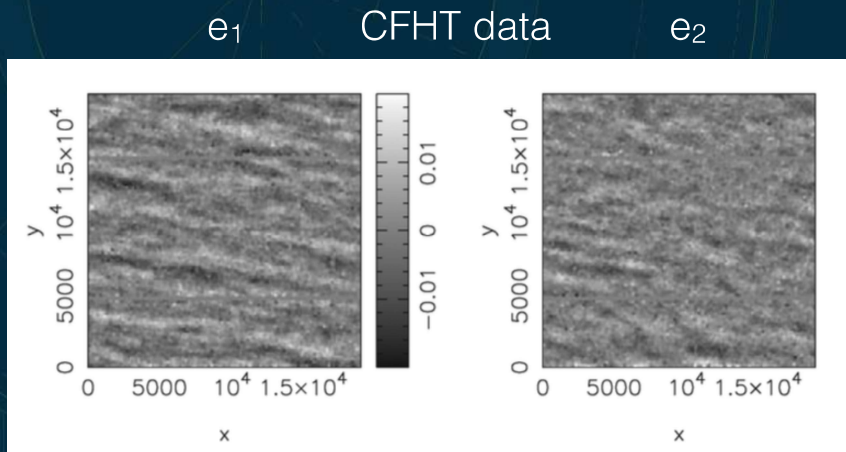
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Fiducial Rubin Obs optical PSF with height variations

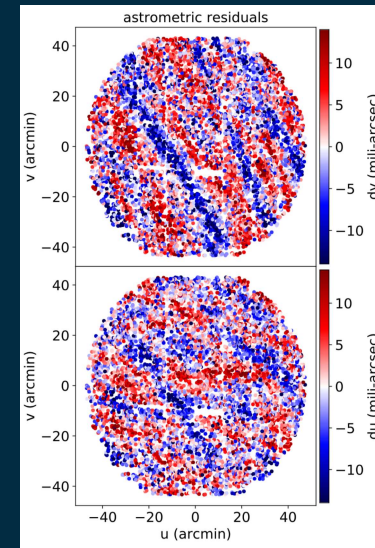


An opportunity: long range correlations

- Atmospheric PSF often contains interesting **anisotropic spatial correlations**
- Most interpolation algorithms can't take advantage of this.
- Proposal is to use a **Gaussian process** with anisotropic kernel to model this.
- Initially interpolate parameters of Von Karman surface brightness profile, but other parameterizations also possible.



Heymans++12



HSC data

Credit: PF Leget

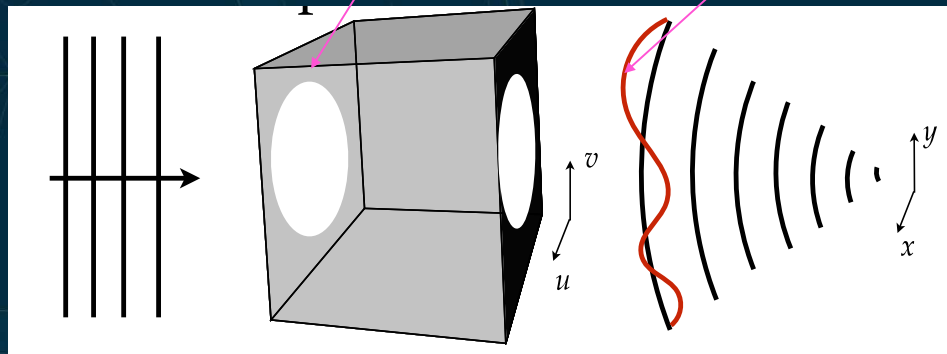
Modeling Strategy

- $PSF = \text{convolve}(\text{optics}, \text{atm}, \text{ccd})$
 - optics = static + dynamic
 - Forward model: fit via chi-square minimization or related.
- Preprocessing: using many donut exposures, fit for static and dynamic optics terms.
 - (Atmosphere is relatively less important for donuts)
- Holding static optics terms fixed, fit an in-focus exposure iteratively:
 - First iteration: degrees of freedom are dynamic optics + uniform atm.
 - Second iteration: hold optics terms fixed and fit individual star atm components.
 - Interpolate atm components (GP?)
 - Repeat as desired.



Optics model - Fourier optics

$$I(\vec{\theta}; \vec{x}) \propto \left| \mathcal{F} \left[\underbrace{P(\vec{\theta}; \vec{u})}_{\text{pupil illumination}} \exp \left(\frac{-2\pi i}{\lambda} \underbrace{W(\vec{\theta}; \vec{u})}_{\text{wavefront}} \right) \right] \right|^2$$



$\vec{\theta}$ = sky
 \vec{x} = image
 \vec{u} = pupil

Wavefront model

Exposure index

Rotation operator

$$W^i(\vec{u}; \vec{\theta}) = \underbrace{W_{\text{tel}}(\vec{u}; \vec{\theta})}_{\text{reference}} + \underbrace{W_{\text{CCD}}(R^i \vec{u}; R^i \vec{\theta})}_{\text{reference}} + \underbrace{W_{\text{visit}}^i(\vec{u}; \vec{\theta})}_{\text{reference}}$$

“reference” wavefront

- Wavefront is the sum of contributions from:
 - **Telescope**
 - static; continuous; may vary quickly over focal plane due to figure errors
 - **CCD height variations**
 - static; contains discontinuities; needs to de-rotate wrt telescope
 - **Per-visit aberrations**
 - dynamic; continuous; slow variation over focal plane; kinds of variations are predictable

Express wavefront as double Zernike series

For one star, pupil wavefront is Zernike series

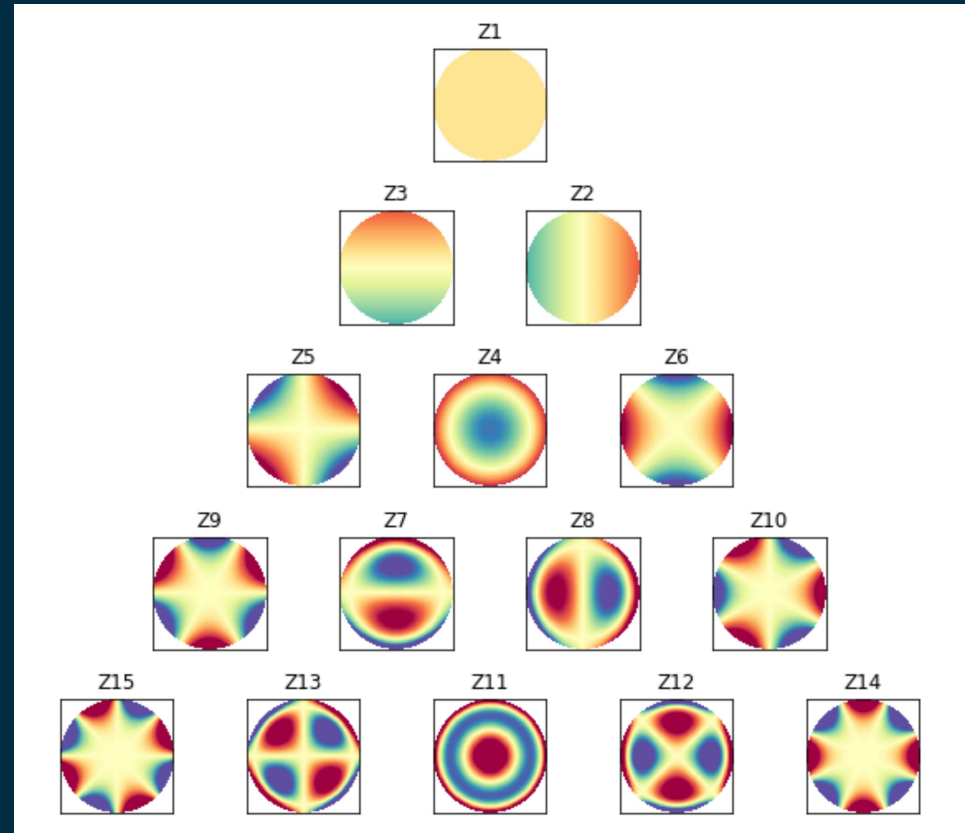
$$W^*(\vec{u}) = \sum_{j=4} a_j^* Z_j(\vec{u})$$

For entire field of view, let coefficient also be Zernike series

$$a_j(\vec{\theta}) = \sum_{k=1} a_{jk} Z_k(\vec{\theta})$$

Double Zernike series

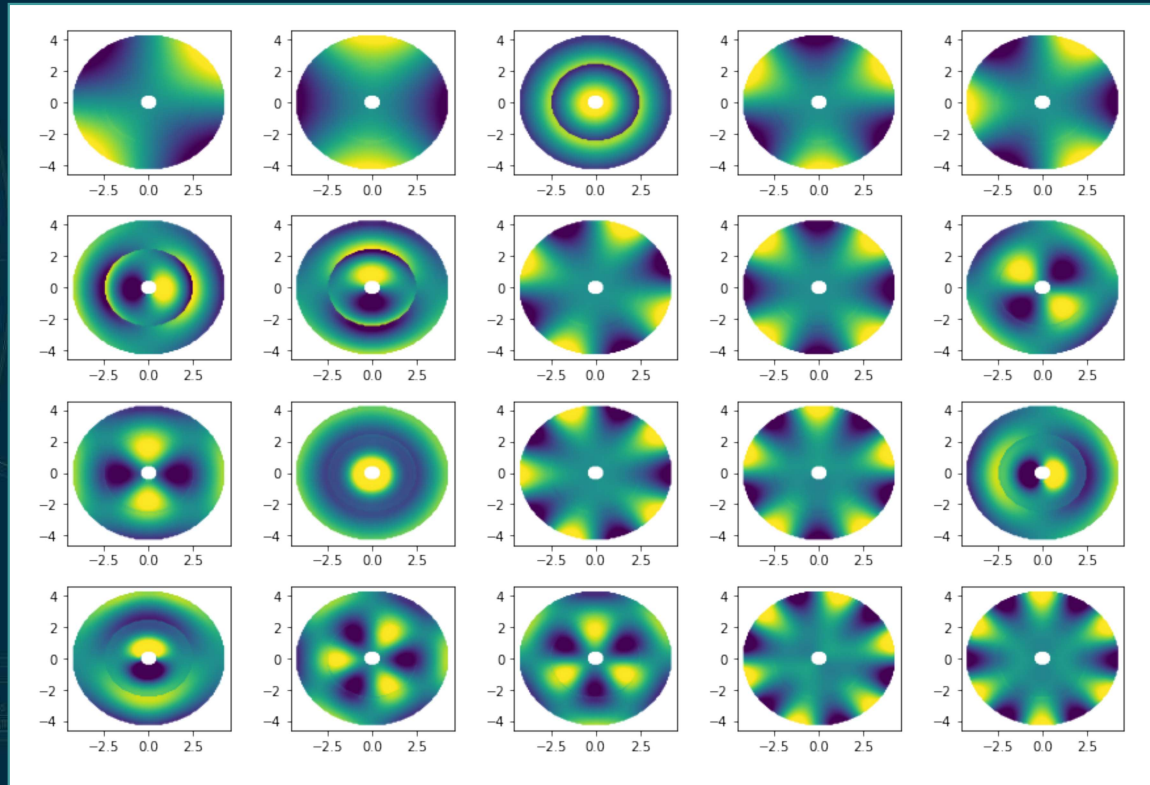
$$W(\vec{u}, \vec{\theta}) = \sum_{j=4} \sum_{k=1} a_{jk} Z_j(\vec{u}) Z_k(\vec{\theta})$$



Misalignments, bending modes introduce low-order patterns

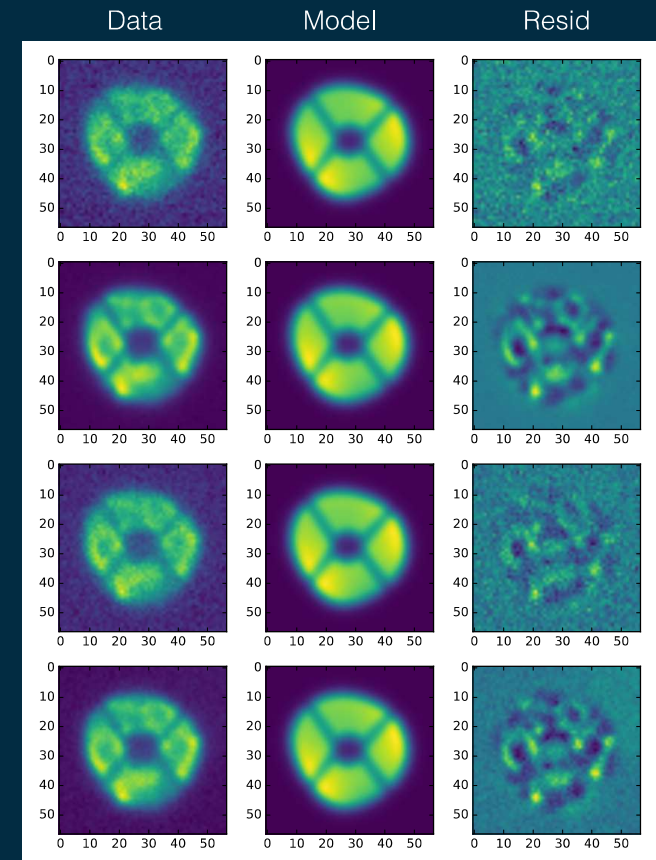
- Dynamic part of optics (flexure) is modelable using only a few low-order double Zernike terms.
- Rigid body of Camera + M2:
 - ~9 DZ terms
- Rigid body + 10 M1M3 modes:
 - ~17 DZ terms
- Rigid body + 20 M1M3 modes:
 - ~34 DZ terms

Bending modes of M1M3



Building the reference wavefront

- Use metrology obtained during construction, or measure directly from **donuts**.
- DECam reference wavefront obtained by low-order detrending to remove flexure followed by taking **mean** of all donut exposure Zernike coefficients.
- Rubin Obs reference wavefront requires two pieces b/c of presence of **rotator**.
- Can solve a large linear algebra problem to obtain.



HSC donuts

Separating wavefront components

- We can take series of donut measurements at different rotator angles to tease apart different contributions to reference wavefront.
- (Don't need to grok this slide now, just here for reference and to show general idea...)

$$\sum_{j=4}^{j_{\max}} a_j^i(\vec{\theta}_*) Z_j(\vec{u}) = \sum_{jk} b_{jk}^{\text{tel}} Z_k(\vec{\theta}_*) Z_j(\vec{u}) + \sum_{jk} c_{jk}^i Z_k(\vec{\theta}_*) Z_j(\vec{u})$$

Annotations for the equation above:

- pink arrow from "geometry" to $Z_k(\vec{\theta}_*)$
- pink arrow from "Note leaving out CCD term" to $Z_j(\vec{u})$
- pink arrow from "have these" to $a_j^i(\vec{\theta}_*)$
- pink arrow from "want these" to b_{jk}^{tel}
- pink arrow from "want these" to c_{jk}^i

- Can solve this for the b's and c's term-by-term (indep for each j)

$$a_j^i(\vec{\theta}_*) = \sum_k b_{jk}^{\text{tel}} Z_k(\vec{\theta}_*) + \sum_k c_{jk}^i Z_k(\vec{\theta}_*)$$

- Matrix equation roughly:

geometry

$$\begin{pmatrix} Z_k(\vec{\theta}_*)'s \end{pmatrix} \begin{pmatrix} b's \\ c's \end{pmatrix} = \begin{pmatrix} a's \end{pmatrix}$$

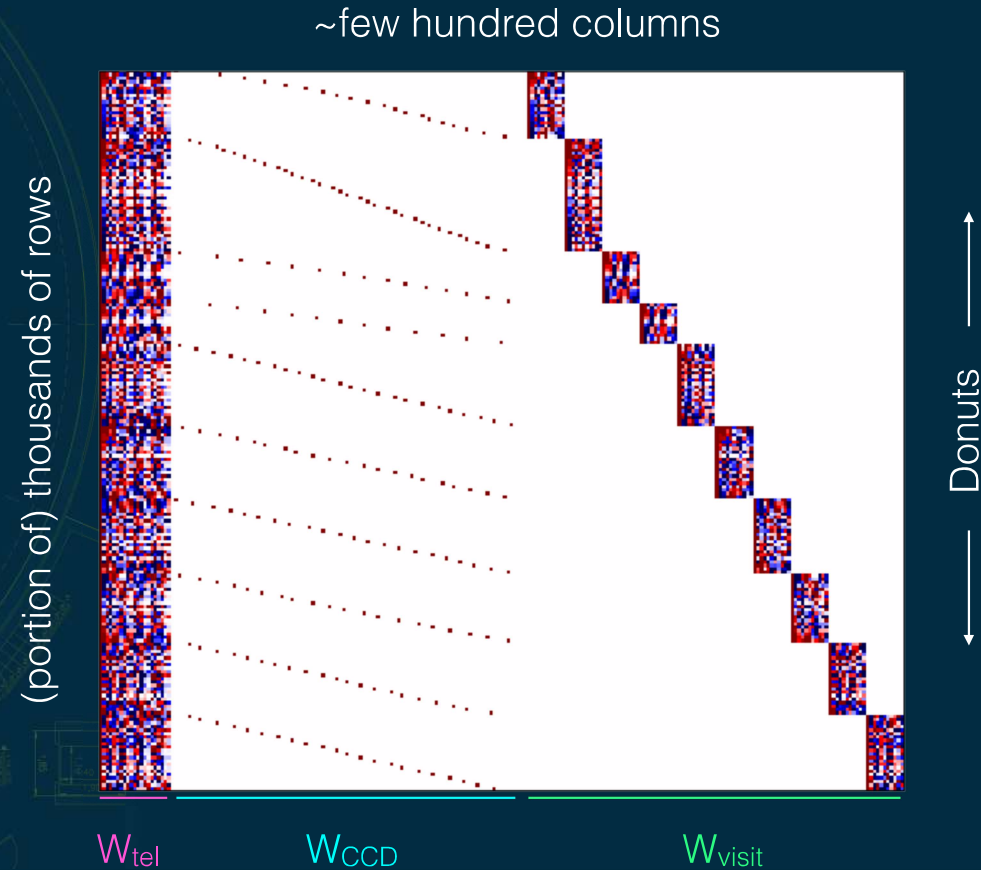
have these

Also require

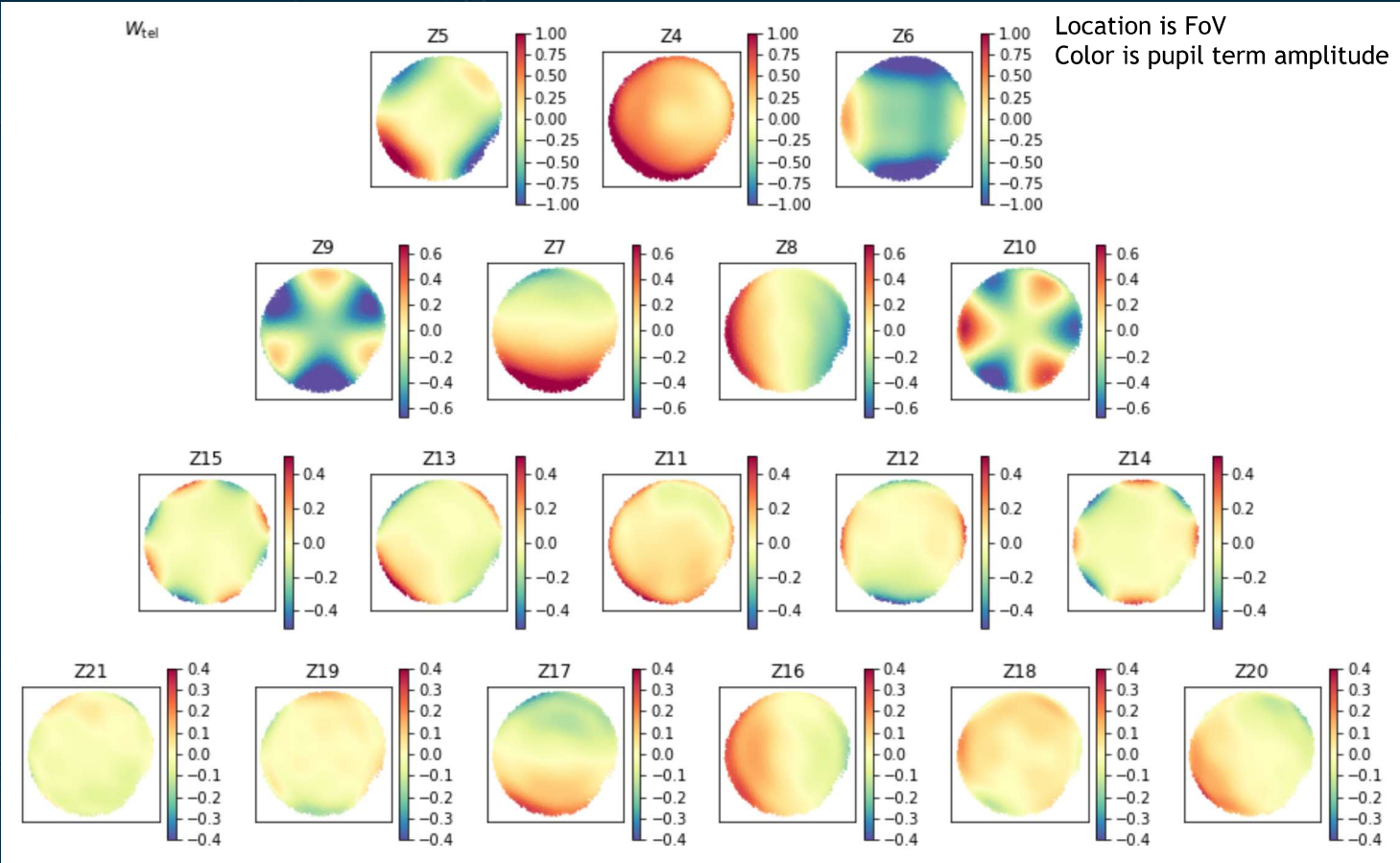
$$\sum_i c_{jk}^i = 0$$

HSC design matrix example

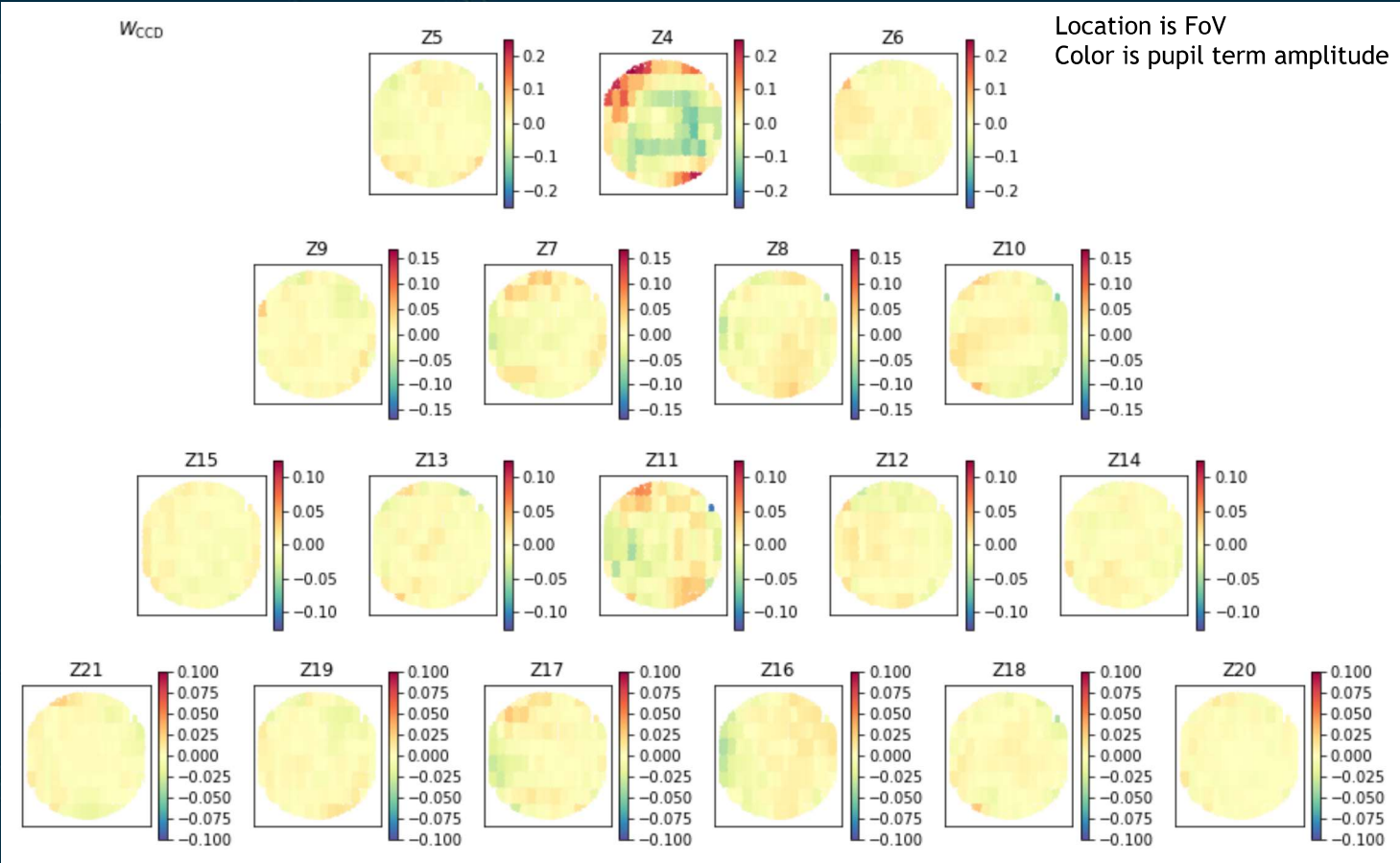
- Color of filled in cells determined by rotator angle and position of * in focal plane.
- All stars contribute to our knowledge of telescope.
- Each star contributes to one CCD term and one per-visit term.
- Visit solutions only good for particular training exposures, but CCD and telescope terms are useful for *all* Rubin obs exposures.
- Repeat for each pupil Zernike coefficient (or pair of related coefficients).



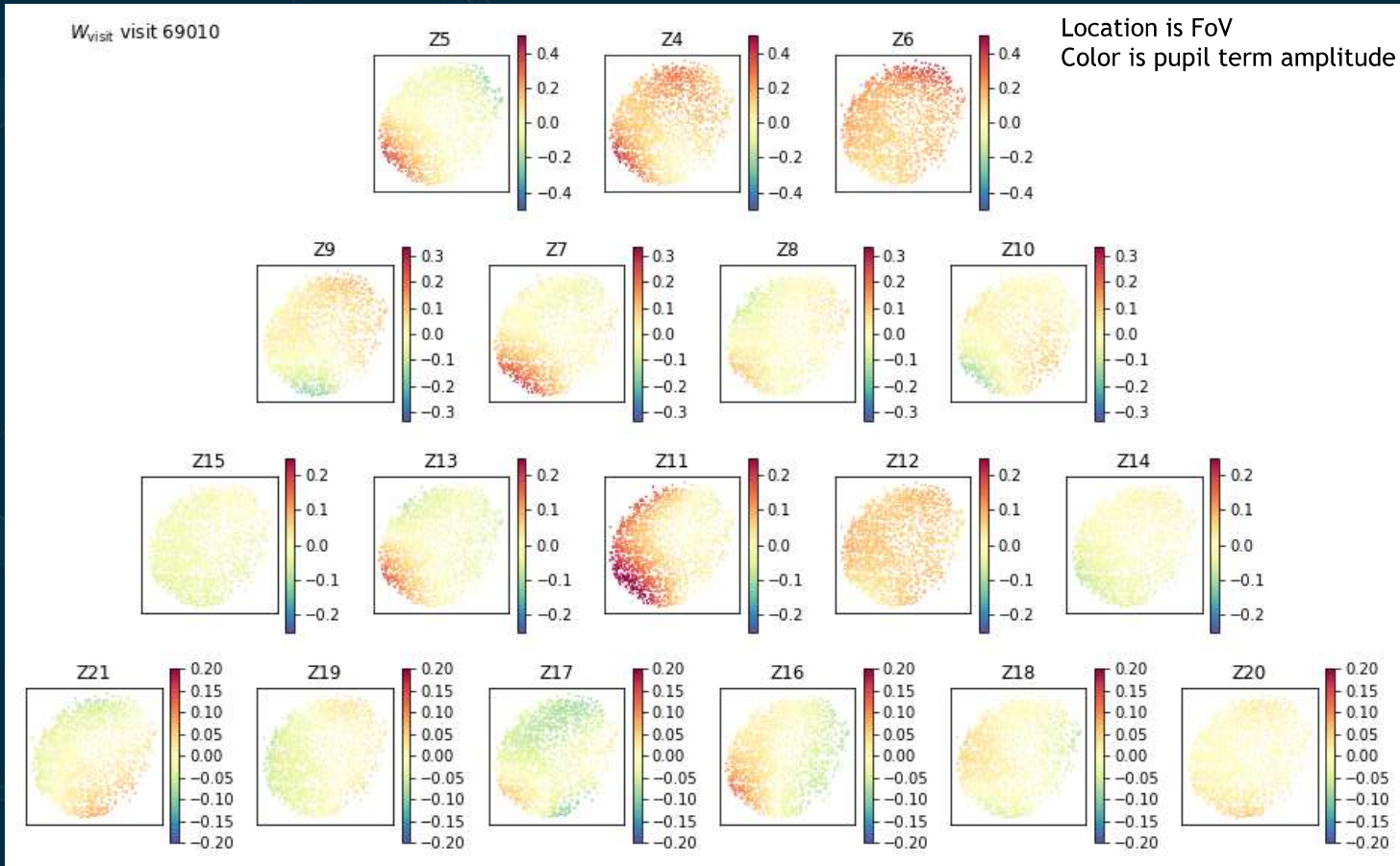
W_{tel} results for HSC



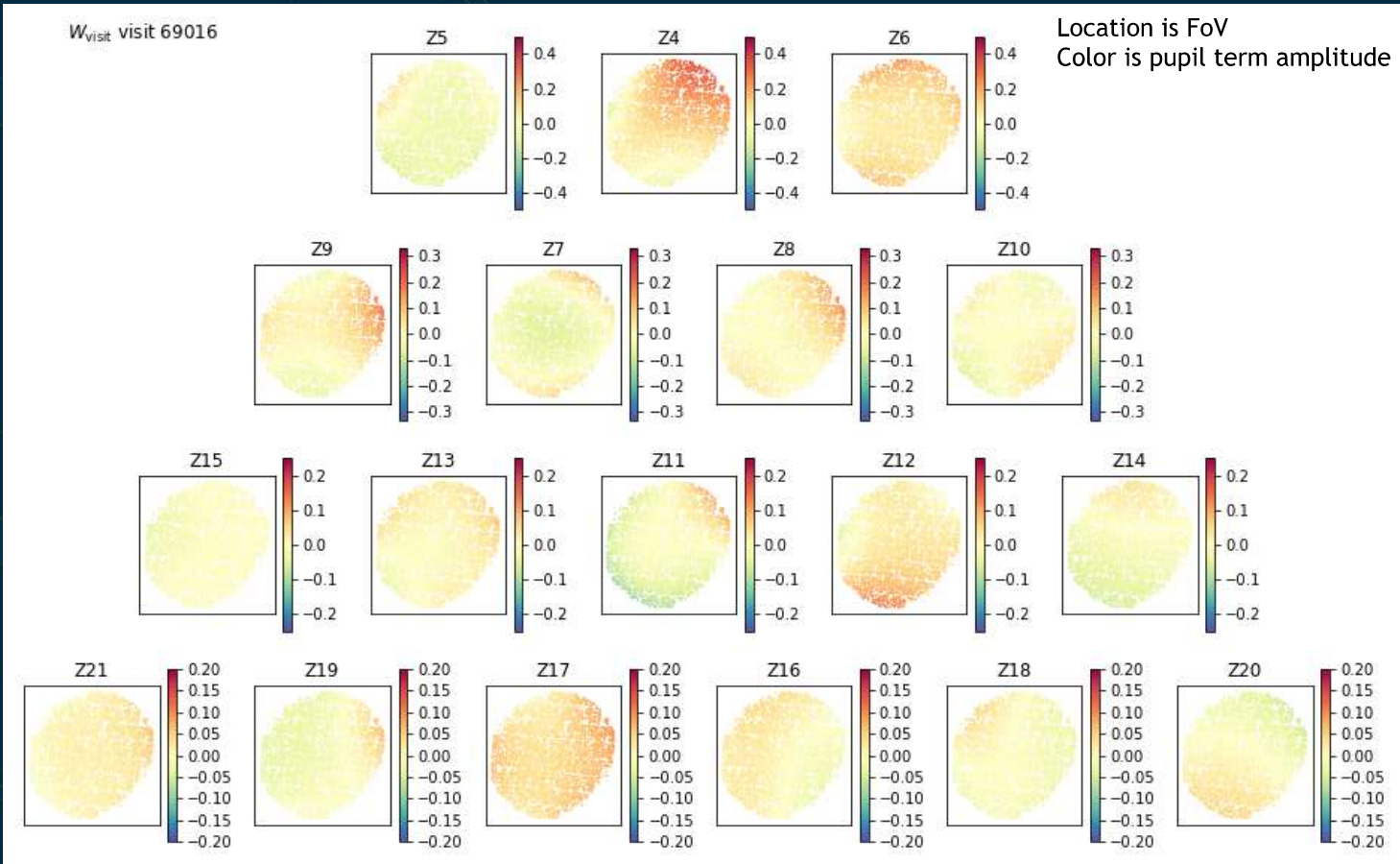
W_{CCD} results for HSC



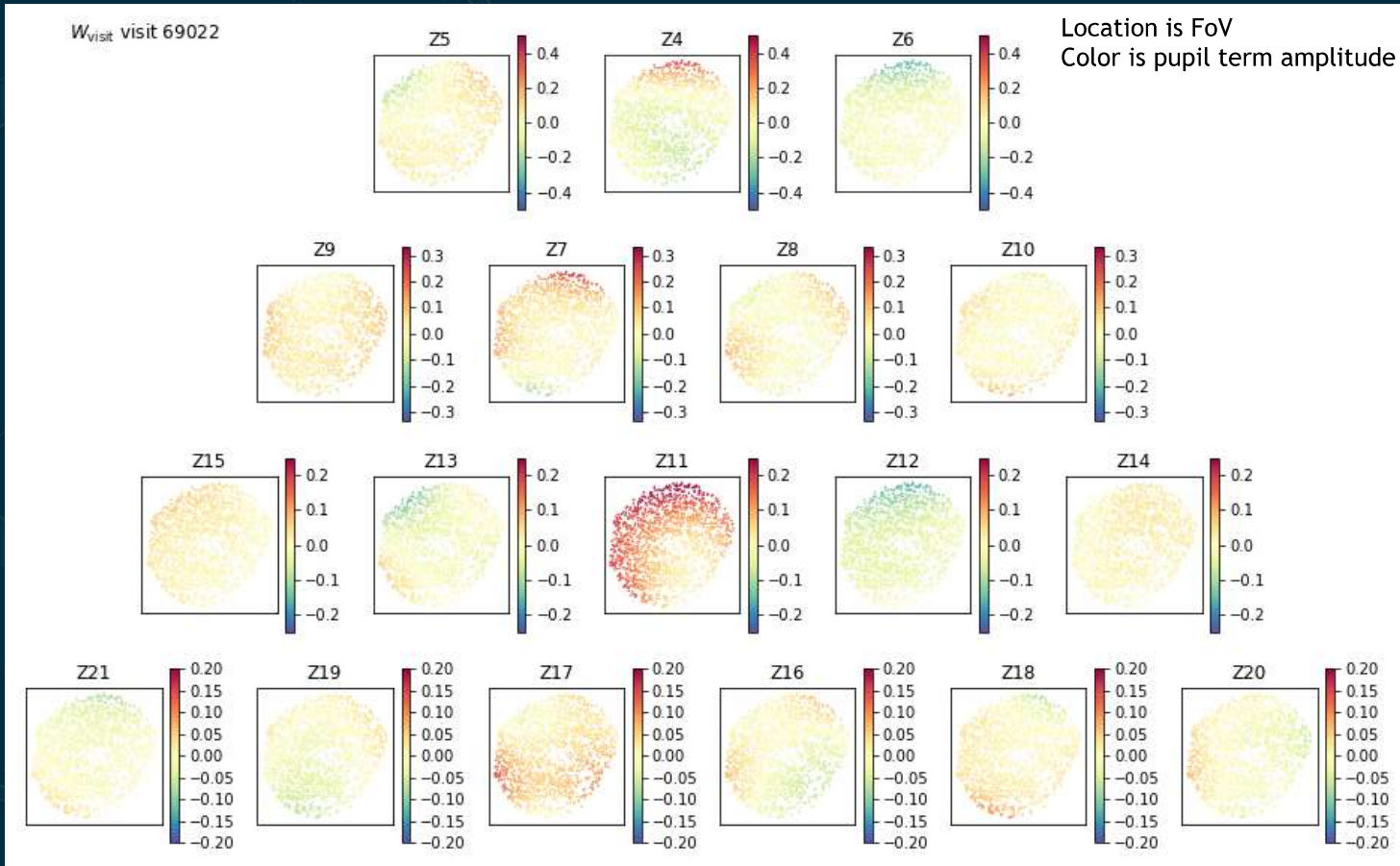
W_{visit} results for a few HSC exposures



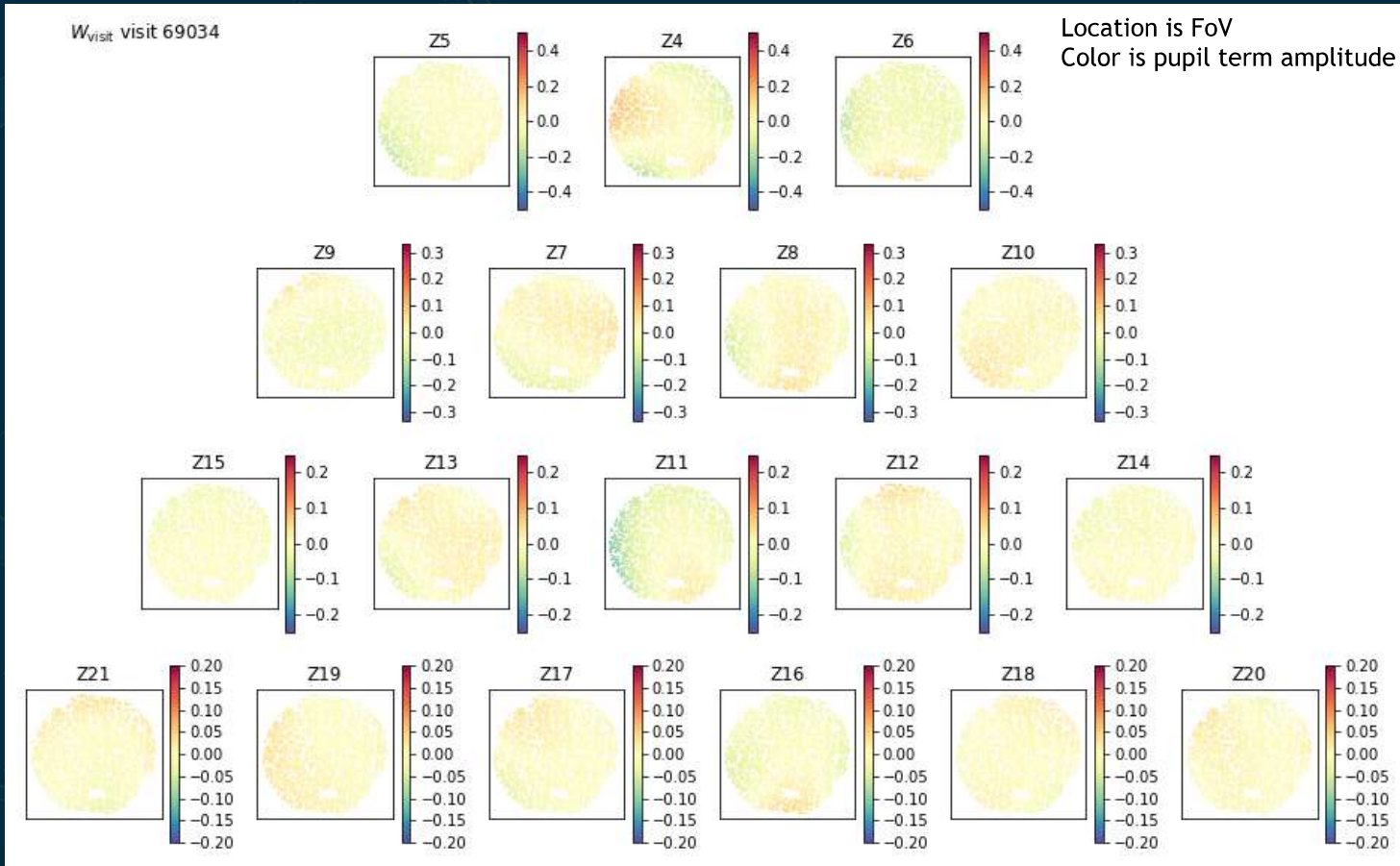
W_{visit} results for a few HSC exposures



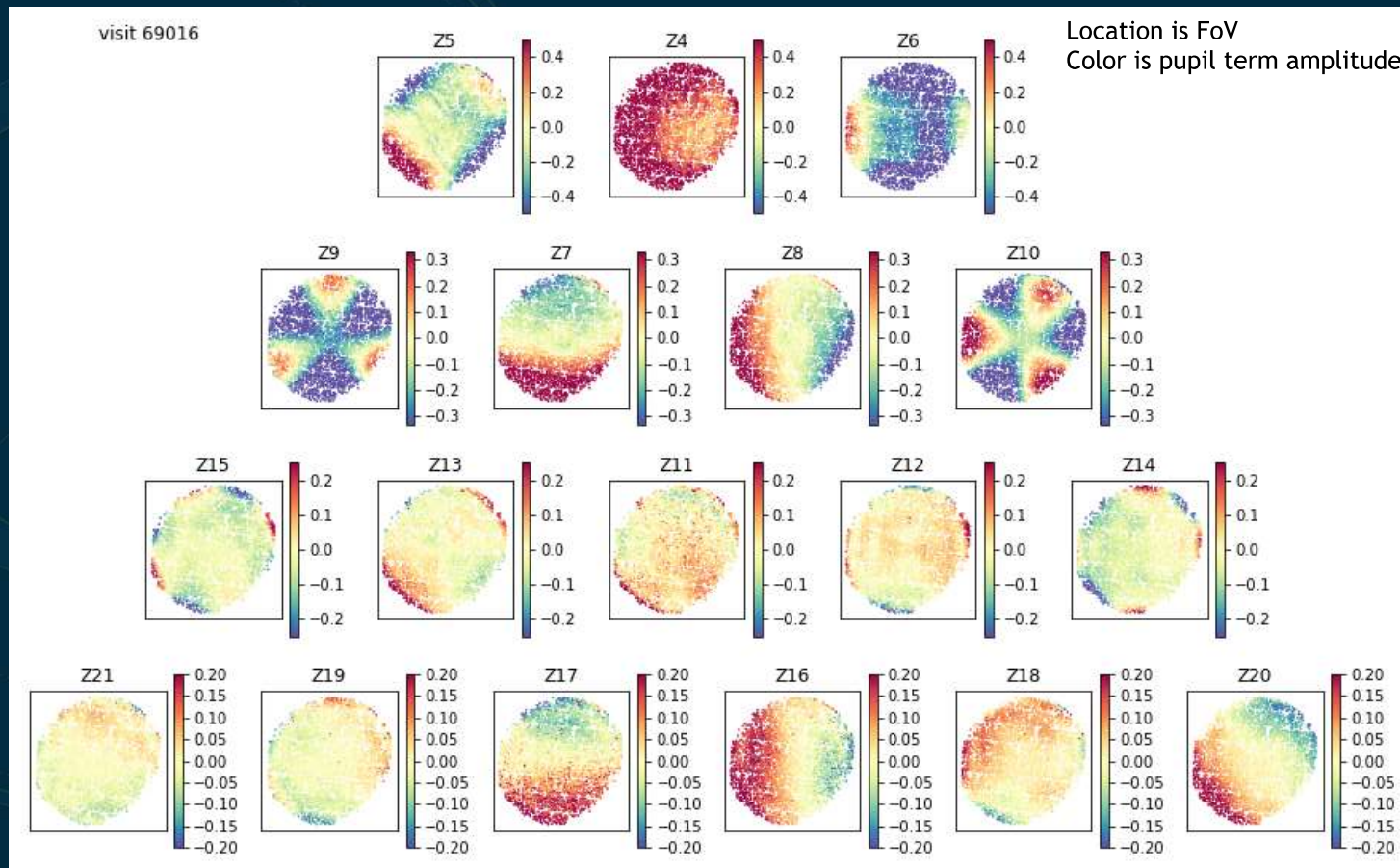
W_{visit} results for a few HSC exposures



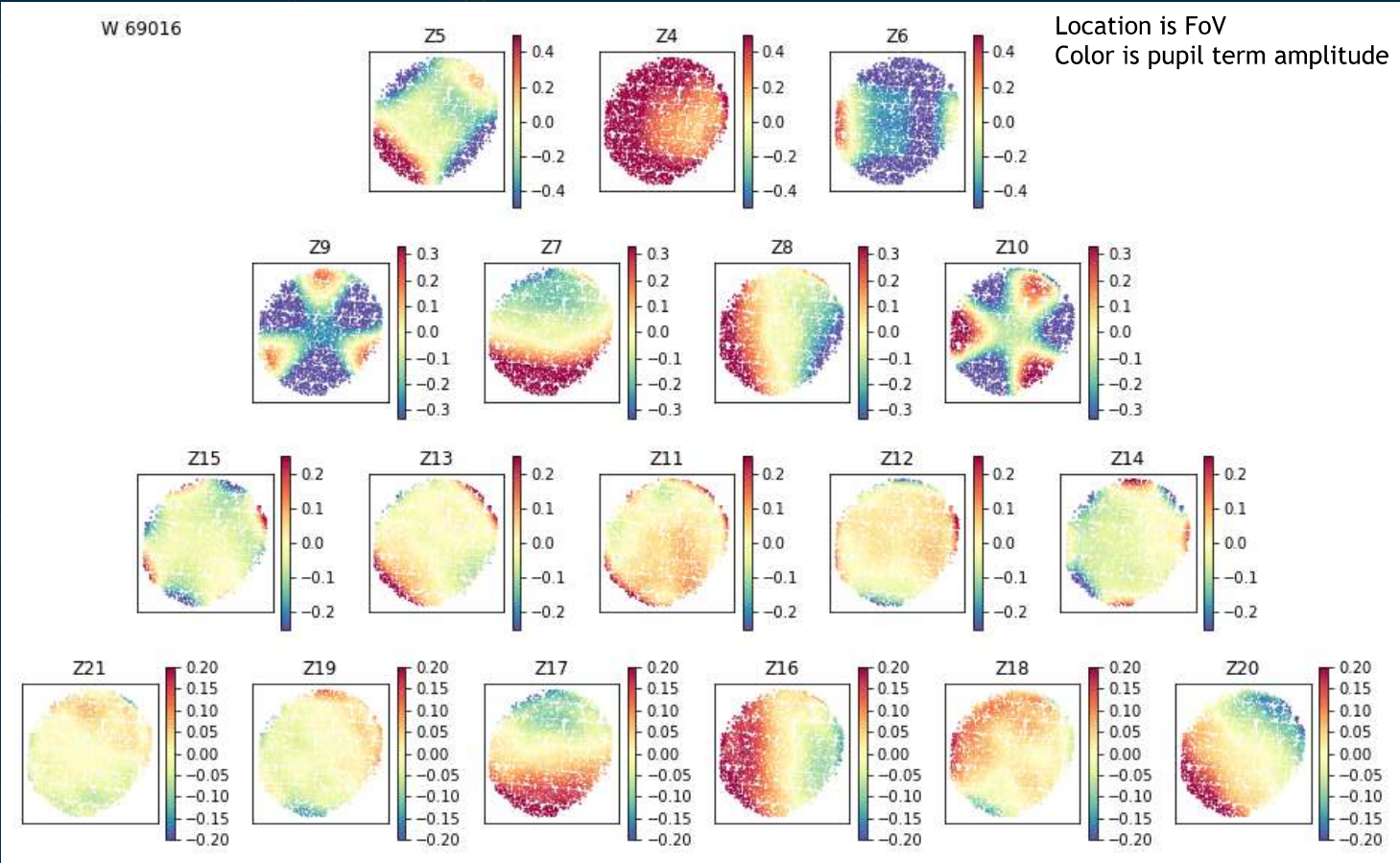
W_{visit} results for a few HSC exposures



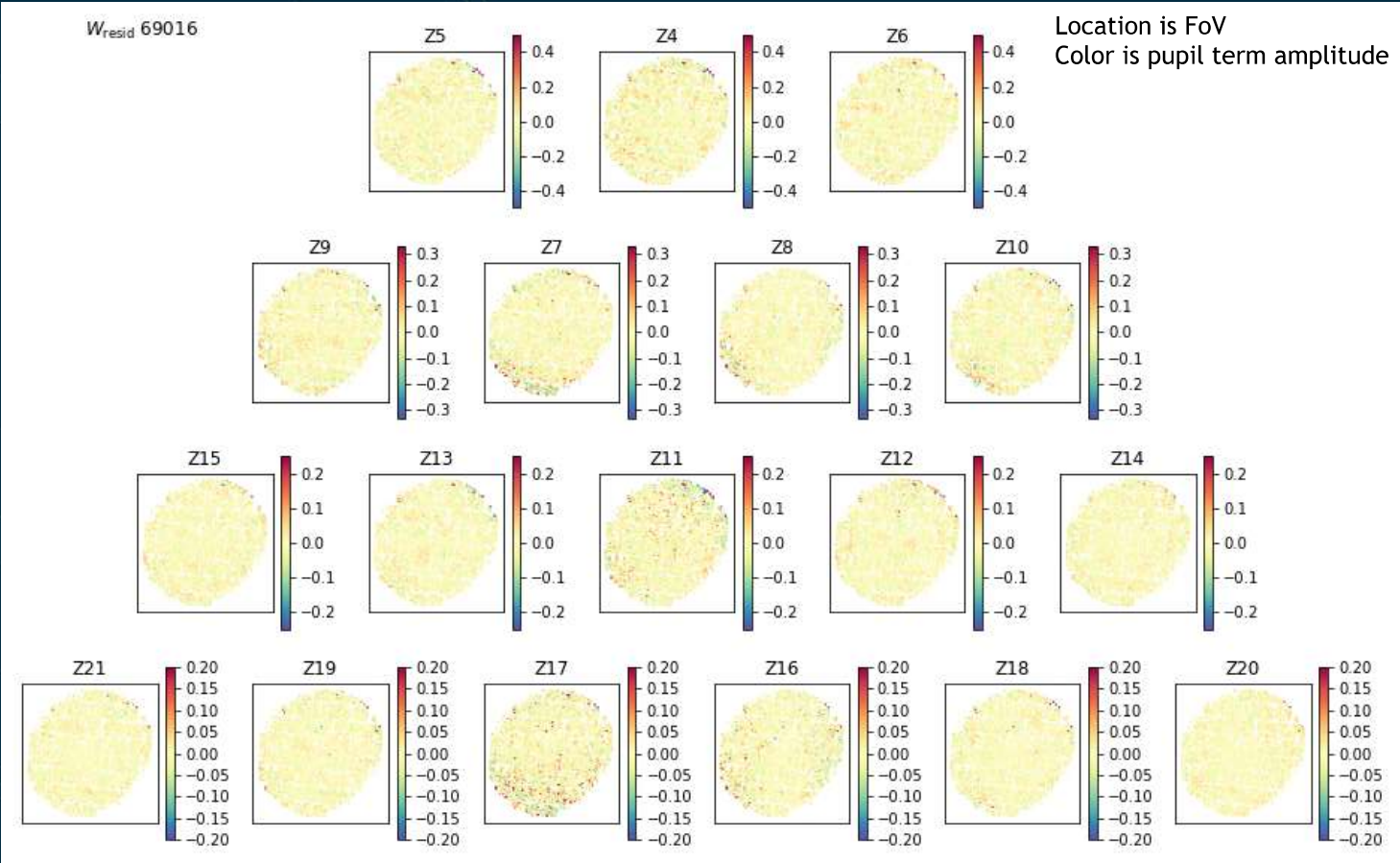
Results for HSC



Results for HSC



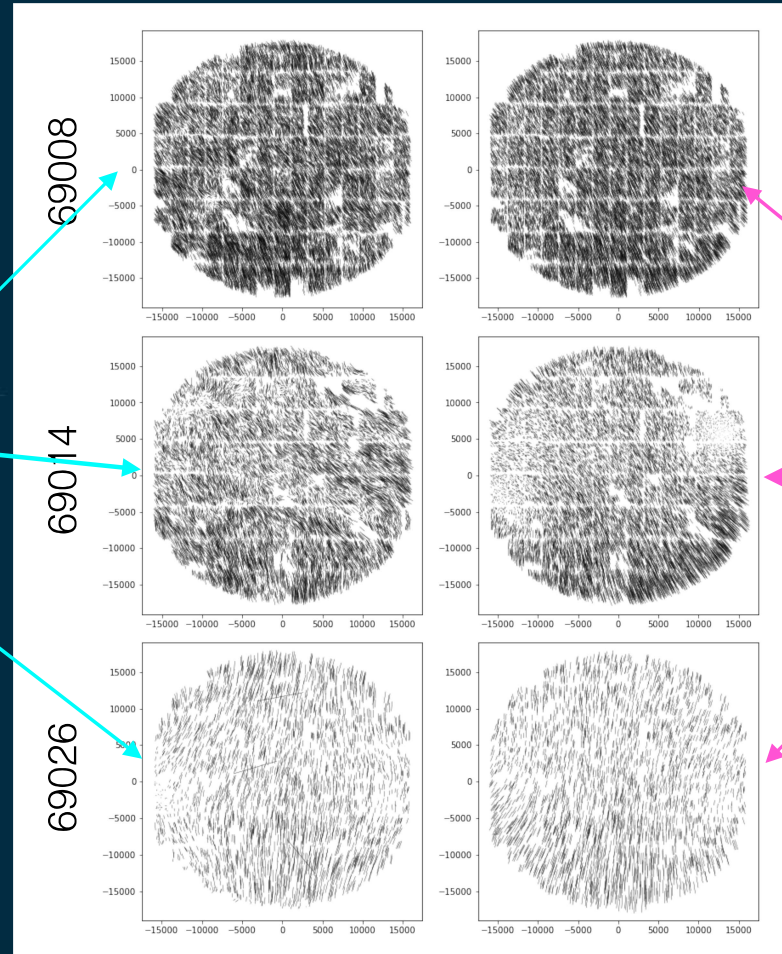
Results for HSC



Results for HSC

- Fitting to new *in-focus* exposures is accomplished by **fixing the static degrees** of freedom inferred from donuts, but **allowing the dynamic degrees of freedom to vary**.
- Can even **learn per-visit degrees of freedom** from principle components of donut exposures.
 - This is model on right: simple uniform-across FoV model for Atm PSF here...
- Generally reasonable output, but HSC limited by small number of donut exposures.
- For Rubin Obs, should also investigate using WF sensors to infer dynamical state.

Data



Rubin
Observatory

Model



Results for DECam

- Dynamic degrees of freedom are a handful of low-order Zernikes here.
- Atm PSF is uniform-across-FoV vonKarman surface brightness profile.
- Capture most of the PSF using **~dozen numbers**.

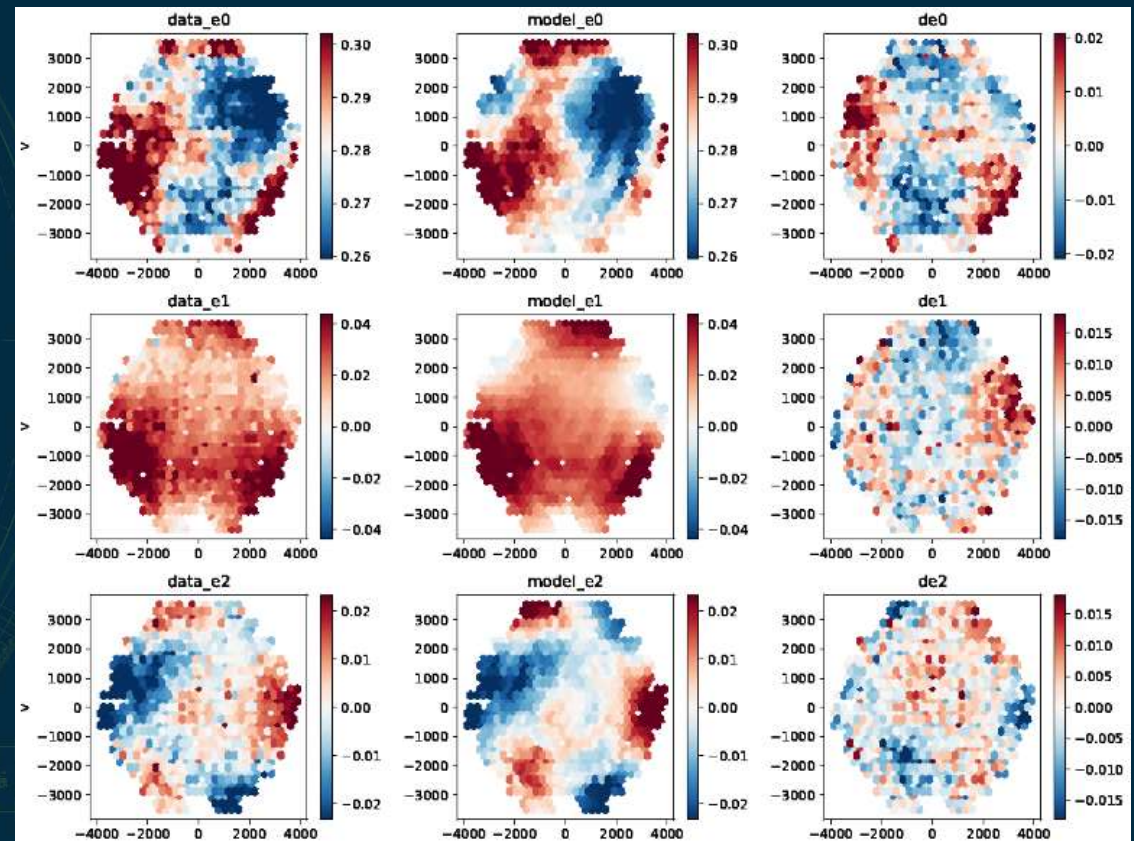


Figure credit: Ares Hernandez

Interpolate atmospheric component with Gaussian Process

- After optics PSF inference:
 - Refit PSF stars, holding optics fixed, allowing atm params to vary independently for each star.
 - Interpolate parameters of atm component using Gaussian Process.
- Gaussian process:
 - Models directly the (potentially anisotropic) correlations in a function instead of the function itself.
 - Pierre-Francois Leget has made significant progress in rapidly modeling correlations.
 - With correlation model in hand, can interpolate from data.
 - Every prediction is a linear combination of data, with relative weights set by model correlation of prediction point with data point (set by displacement between prediction and data point)
 - Many approximate GPs exist with speedier maths.



Piff

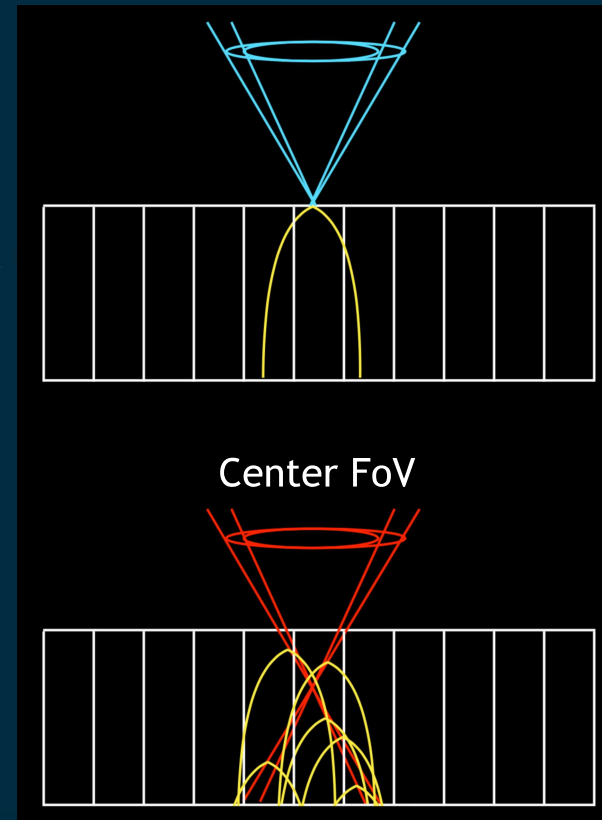
- Mike showed earlier that Piff is already superior to PSFex for DES
- Framework for modular PSF is now being developed in Piff
- We are planning to integrate Piff into the DM stack. →
- Two tasks:
 - 1) Ability to run Piff on Rubin Obs images (already demonstrated by Mike with DC2 images)
 - 2) Ability to use Piff PSF outputs in subsequent stack measurement algorithms.



Chromatic effects

- $PSF = PSF(\lambda)$
- There are many:
 - Differential chromatic refraction
 - Chromatic seeing
 - Dispersive optics
 - Diffraction
- Absorption length of silicon coupled with:
 - fast beam
 - charge diffusion
 - lateral electric fields
- Reflections off backside of silicon.

Josh's favorite chromatic effect:
silicon absorption length + fast beam



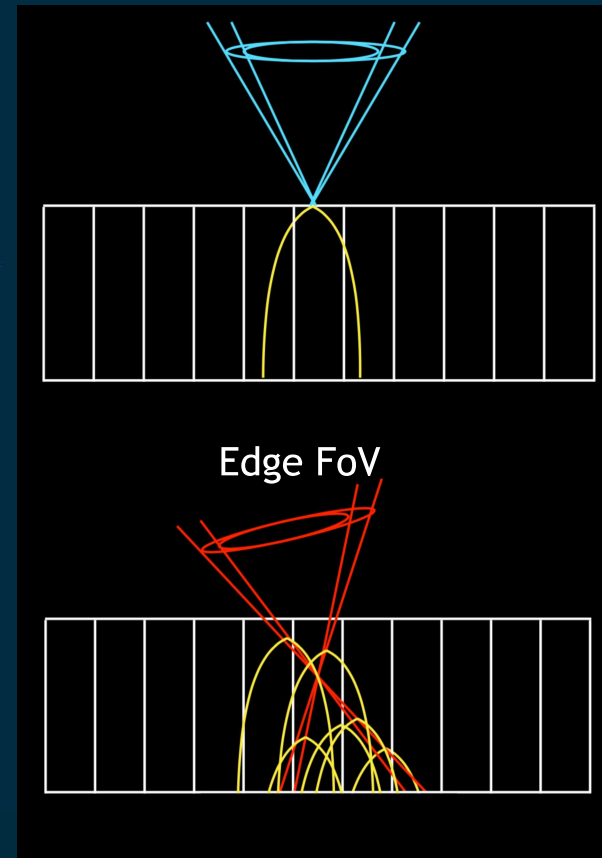
In blue, all photons
convert at surface

In red, redder photons
convert deeper, and b/c
converging beam, over
different range laterally.

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Modeling chromatic effects

- Keep in mind that **stars are “easy.”** Their SEDs are essentially a **one-parameter family** (temperature).
- We have good models for many individual components of $\text{PSF}(\lambda)$ (optics/atm/ccd/etc).
- I have confidence **we can infer $\text{PSF}(\lambda)$.**
 - Fallback option: Piff PixelGrid regressed on color. (2x params; enough stars?)
- **Hard part** is inferring galactic SEDs from photometry to construct PSF to use in **galaxy** measurements.
 - This is similar to photo-zs, except no catastrophic outliers.
- The zero-order solution is to **model SEDs linearly across bands** using neighboring bands' colors.
- There's an interesting question for meta-detection, part of which uses a single PSF by which to deconvolve a small scene of objects with potentially disparate SEDs.



Conclusions

- Let's adopt Piff!
 - Better than PSFex
 - Has room for baseline chromatic PSF
- Making progress with wavefront model, but still work to be done.

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